## MTH 111, Math. for the Architects, Exam I, Spring 2014

Ayman Badawi

## (Each question = 10 points, total points 100 points)

**QUESTION 1.** Find an equation of the ellipse with the vertices (4,3), (1,7), and (-2,3). Find the constant k. Find the foci. Make a rough sketch of such ellipse.

**QUESTION 2.** Find an equation of the hyperbola that is centered at (2, 1) and with constant k = 6 such that (2, 6) is one of the foci. Find the second foci, find the vertices, and make a rough sketch of such hyperbola.

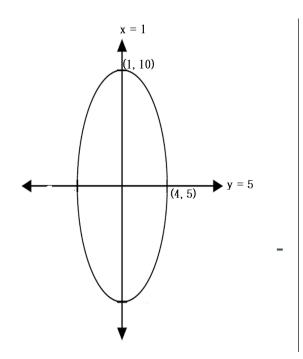
**QUESTION 3.** Given x = 1 is the directrix line of a parabola that passes through the point (6, 5) and the line y = 2 passes through the vertex of the parabola. Find the vertex, the focus, and make a rough sketch of such parabola. Then find an equation of the parabola. [Hint: there are two such parabolas, just find one]

**QUESTION 4.** Find the directrix, the focus, and the vertex of the parabola  $y = 0.5(x+5)^2 + 4$ 

**QUESTION 5.** Find the foci, the constant k, and the vertices of the ellipse  $(x+2)^2/25 + (y-3)^2/9 = 1$ 

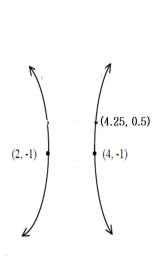
**QUESTION 6.** Find the center, the foci, the vertices of the hyperbola  $x^2 - 2y^2 - 4y = 18$ 

QUESTION 7. Find the foci, and the equation of the below ellipse:





Find the foci, and the equation of the below hyperbola:



**QUESTION 9.** Find an equation of the plane P that contains the line L: x = t, y = 1 - t, z = 2t and the point Q = (1, 0, 5) [note that the point Q does not lie on L]

**QUESTION 10.** a) Find the distance between the point Q = (2, 2, 1) and the plane x + 3y + 5z = 15

b) The line  $L_1: x = 5t, y = 4 - t, z = 3 + t$  intersects the line  $L_2: x = 1 + 2s, y = 9 - 3s, z = 2s$  at a point Q. Find Q

## **Faculty information**

Ayman Badawi, Department of Mathematics & Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates. E-mail: abadawi@aus.edu, www.ayman-badawi.com